

## AS Level / Year 1 Custom Mock 2

December 2017 Mocks



Question	Scheme	AO	Marks	
1				
	$(3-k)^2 - 4(k)(-4) = 0$ Uses the discriminant	AO1.1a	M1	
	$\Rightarrow k^{2} + 10k + 9 = 0 \Rightarrow k =$ Forms a 3TQ and attempts to solve their 3TQ	AO1.1a	dM1	
	k = -1, k = -9 Scores 3/3.	AO1.1b	A1	
			3	
	Question 1 Notes			
1 <sup>st</sup> M1 – this	mark is for substituting the values of $a$ , $b$ and $c$ from the quadratic into $b^2 - 4ac \{=0\}$ . Looking for the	correct exp	pression	
only, so igno	pre <,>, $\leq$ , $\geq$ . Condone sign errors in substituted values of $a, b$ and $c$ .			
2 <sup>nd</sup> M1 – this mark is for forming a 3TQ and attempting to solve it using factorising, completing the square or the quadratic formula. This is dependent on the 1 <sup>st</sup> M1				
A1 – correct	values of <i>k</i> , both values must be present to score the marks.			

Question	Scheme	AO	Marks		
2					
(a)	$\sqrt{a} + 2\sqrt{a} = 3$ Uses $a^{\frac{1}{2}} = \sqrt{a}$ oe Uses $\sqrt{4a} = 2\sqrt{a}$ oe	AO1.1a AO1.1a	M1 M1		
	$\sqrt{a} = 1 \Rightarrow a = 1$ Correct solution only	AO1.1b	A1		
			3		
	Question 2 Notes				
1 <sup>st</sup> M1 – use	1 <sup>st</sup> M1 – uses $a^{\frac{1}{2}} = \sqrt{a}$ OR $\sqrt{4a} = (4a)^{\frac{1}{2}}$				
2 <sup>nd</sup> M1 – use	$2^{nd}$ M1 – uses $\sqrt{4a} = 2\sqrt{a}$ OR $(4a)^{\frac{1}{2}} = 2a^{\frac{1}{2}}$				
A1 – correct	solution only. Additional solutions score A0				

Question	Scheme	AO	Marks
3			
Method 1	$\frac{2-x}{x} < 3 \Rightarrow x(2-x) < 3x^2$ Multiplies by $x^2$ . For multiplication by x, see special case in notes	AO1.1a	M1
	$2x^2 - x > 0$ Obtains the correct inequality oe	AO1.1b	A1 oe
	CVs $x = 0$ , $x = \frac{1}{2}$ CVr $x = 0$ , $x = \frac{1}{2}$	AO1.1b	A1
	Solution set = $\begin{cases} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\$	AO1.1a	M1
	$\Rightarrow \text{ Solution set} = \left\{ x : x < 0 \text{ or } x > \frac{1}{2} \right\}$ Correct solution set. Other equivalent formulations of the set should be accepted	AO1.2	A1FT
			[5]
Method 2	2-x $2-x$ Attempts a common denominator	AO1.1a	M1
	$\frac{x}{x} \xrightarrow{x} x x \xrightarrow{x} x x x x x x x x x x x x x x x x x x $	AO1.1b	A1
	Case 1: $2-4x < 0$ and $x > 0$ $\{\Rightarrow x > \frac{1}{2}\}$ Identifies the two correct cases	AO1.1b	A1
	Case 2: $x < 0$ and $2 - 4x > 0 \{ \Rightarrow x < 0 \}$		
	$\Rightarrow \text{Solution set} = \begin{cases} r \mid r < 0 \text{ or } r > 1 \end{cases}$ Method to find solution set	AO1.1a	M1
	$\Rightarrow$ solution set $= \begin{bmatrix} x \cdot x < 0 \text{ of } x > \frac{\pi}{2} \end{bmatrix}$ Correct solution set. Other equivalent formulations of the set should be	AO1.2	A1FT
	$OR \left\{ x : x < 0 \right\} \cup \left\{ x : x > \frac{1}{2} \right\}$		[5]
			5

	Question 3 Notes
SPECIAL C	ASE:
Multiplication	h by x can score M0 A0 A0 M1 A1FT max.
2 <sup>nd</sup> M1 for at	tempting to solve their linear inequality (most probably, $2 - x < 3$ ).
3 <sup>rd</sup> A1 for co	rrect solution set following their inequality i.e. $\{x : x < -1\}$ (oe).
Method 1:	
1 <sup>st</sup> M1 – can	also see multiplication by $x^4$ , $x^6$ , etc., which can score the M1.
1 <sup>st</sup> A1 – for tl inequality for	he correct <b>quadratic</b> inequality. Candidates that multiply by higher powers must reduce their inequality to a quadratic r this mark. This can be implied by the correct CVs.
2 <sup>nd</sup> A1 - corr	rect CVs. Additional CVs is A0.
2 <sup>nd</sup> M1 – this appropriate g	s is not a dependent method mark. This is for an attempt to solve their inequality. This can be done through use of an graph, for example; sketching the appropriate graph and indication of the relevant region is M1.
3 <sup>rd</sup> A1FT – th condoned.	his is for the correct solution set. The set can be expressed in any correct way. Use of $x$ instead of $x \in \mathbb{R}$ should be This is ft their <b>quadratic</b> inequality.
Method 2:	
1 <sup>st</sup> M1 – atte	mpts to form a correct common denominator with all terms on one side of the inequality.
$1^{st} A1 - for c$	correct workings so far (i.e. correct inequality obtained)
2 <sup>nd</sup> A1 – use	s cases to solve the inequality.
2 <sup>nd</sup> M1 – this set/range of	is not a dependent method mark. This is for an attempt to find the correct solution set. It is for an attempt to find the values that satisfy <b>both</b> restrictions (if appropriate) and then taking the union of their corresponding sets.
3 <sup>rd</sup> A1 FT – t condoned.	this is for the correct solution set. The set can be expressed in any correct way. Use of x instead of $x \in \mathbb{R}$ should be This is ft finding the intersection of their two restrictions on x

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Question	Schen	ne	AO	Marks
4				
<b>(a)</b> Method 1	$2^{2(6-3x)} = 2^{3(2y)}$	Attempts to convert both sides into base 2. Can be implied	AO1.1a	M1
	$2(6-3x) = 3(2y) \Longrightarrow y = 2-x$	Correct expression	AO1.1b	A1 <b>[2]</b>
<b>(a)</b> Method 2	$\log(4^{6-3x}) = \log(8^{2y}) \Longrightarrow (6-3x)\log 4 = 2y\log 8$	Takes logs (any base) <b>and</b> uses the power rule	AO1.1a	M1
	$6-3x = \frac{3}{2}(2y) \Longrightarrow y = 2-x$	Correct expression	AO1.1b	A1 <b>[2]</b>
<b>(b)</b> Method 1	$(x-2)^{2} + 9(2-x)^{2} = 10$	Substitutes <b>their</b> <i>y</i> in terms of <i>x</i> into the second equation	AO2.2	M1
	$x^{2} - 4x + 4 + 9(4 - 4x + x^{2}) = 10$	Expands brackets and attempts to form a 3TQ	AO1.1a	dM1
	$\Rightarrow x^2 - 4x + 3 = 0$	Correct quadratic expression	AO1.1b	A1
	So $x = 1, 3$	Correct values of <i>x</i>	AO1.1b	A1
	When $x = 1 \Rightarrow y = 1$	Substitutes their $x$ to find $y$	AO1.1a	dM1
	When $x = 3 \Rightarrow y = -1$	Correct values of $x$ and $y$	AO1.1b	A1
				[6]

<b>(b)</b> Method 2	$(2-y-2)^2 + 9y^2 = 10$	Substitutes for $x$ in the equation	AO2.2	M1		
	$y^2 + 9y^2 = 10 \implies 10y^2 - 10 = 0$	Attempts to form a 3TQ	AO1.1a	dM1		
		Correct 3TQ	AO1.1b	A1		
	So <i>y</i> =-1, 1	Correct values of y	AO1.1b	A1		
	When $y = 1 \Longrightarrow x = 1$	Substitutes their $y$ to find $x$	AO1.1a	dM1		
	When $y = -1 \Rightarrow x = 3$	Correct values of $x$ and $y$	AO1.1b	A1		
				[6]		
				8		
		Question 4 Notes	·			
(a) Method						
M1 – attemp	ts to covert both sides of the equation to base 2. C	condone errors like $\left(a^{b} ight)^{c}=a^{b+c}$ . This can be implied – f	for example,	, by a		
correct equation.						
(a) Method 2	(a) Method 2					
M1 – takes l	v11 – takes logs and uses the power rule. Candidates can use any base.					

Question	Scheme		AO	Marks
5				
(a)	$f(4) = -2(4)^{3} + 9(4)^{2} - (4) - 12$ = -128 + 144 - 4 - 12 = 0 ∴ the curve y = f(x) crosses the x axis when x = 4	Substitutes 4 into f <b>and shows</b> that it is equal to 0 (all of the terms or groups of terms must be evaluated) <b>and</b> concludes: 'therefore, it crosses {the <i>x</i> axis} when <i>x</i> = 4' oe	AO2.1	B1 [ <b>1</b> ]
(b) Method 1	$ \frac{-2x^{2} + x + 3}{x - 4 - 2x^{3} + 9x^{2} - x - 12} - \frac{-2x^{3} + 8x^{2}}{x - 12} + 1x^{2} - 1x  (*) + \frac{1x^{2} - 4x}{3x - 12} - \frac{3x - 12}{0} $	Attempts to find the other quadratic factor by long division All working leading up to and including the line (*) correct, including the $-2x^2$ in the quotient	AO1.1a AO1.1b	M1 A1
	$f(x) = (x-4)(-2x^2 + x + 3)$ = -(x-4)(2x-3)(x+1)	Attempts to factorise <b>their</b> quadratic factor Correct factorisation oe (e.g. accept –ve sign distributed into one of the factors)	AO1.1a AO1.1b	dM1 A1 <b>[4]</b>

(b) Method 2	$f(x) = (x-4)(-2x^2 + bx + 3)$ Attempts to find outQuadratic factor	t quadratic factor using inspection factor of the form $2x^2 + bx + 3$	.1a .1b	M1 A1
	$f(x) = (x-4)(-2x^2 + x + 3)$ $= -(x-4)(2x-3)(x+1)$ Attempts to factorise Correct factorisation -ve sign distribution	e <b>their</b> quadratic factor n oe (e.g. accept buted into one of the factors)	.1a .1b	dM1 A1 <b>[4]</b>
(c)	$x-4 = -1, \frac{3}{2}, 4$ $\Rightarrow x = 3, \frac{11}{2}, 8$ Sets $x-4$ equal to at roots of the constant	t least one of the AO2 their graph in (c) prrect values of <i>x</i> AO1	2.2 .1b	M1 A1 <b>[2]</b>
	Question 5 Notes			7

(a) B1 – substitutes 4 into f, **shows** that it is 0 and then gives a conclusion. At least some of the terms have to be evaluated here, either individually or in groups. For example,

 $f(4) = -2(4)^3 + 9(4)^2 - (4) - 12 = 0$  is NOT enough and scores B0, but  $f(4) = -2(4)^3 + 9(4)^2 - (4) - 12 = 16 - 16 = 0$  is OK

The conclusion requires something simple: 'therefore, it crosses the x axis at 4' oe

(b) Method 1:

 $2^{nd}$  M1 – writes their factor  $ax^2 + bx + c = (px + r)(qx + s)$ , where  $pq = \pm a$ ,  $rs = \pm c$  (M0 if their quadratic factor is irreducible)

(b) Method 2:

1<sup>st</sup> M1 – attempts to find the quadratic factor by inspection. This mark is awarded for one the coefficients of the quadratic factor correct.

 $1^{st} A1$  – their quadratic factor of the form  $-2x^2 + bx + 3$  for some number **or letter** *b*.

 $2^{nd}$  M1 – writes their factor  $ax^2 + bx + c = (px + r)(qx + s)$ , where  $pq = \pm a$ ,  $rs = \pm c$  (M0 if their quadratic factor is irreducible)

Question	Scheme		AO	Marks
6				
(a/i)	e.g. $5x + 2(2 - x) = 3 \implies x =$	Eliminates one variable from the two equations of the circles	AO3.1a	M1
	$x = -\frac{1}{3}, y = \frac{7}{3}$	Correct centre of the circle. Accept coordinates etc.	AO1.1b	A1 <b>[2]</b>
(a/ii)	$(x-2)^{2} - 4 + (y+1)^{2} - 1 = 0$	Completes the square on both <i>x</i> and <i>y</i> terms	AO1.1a	M1
	Radius is $\sqrt{5}$	Correct radius oe	AO1.1b	A1 <b>[2]</b>
(b)	Distance between centre and A is $\sqrt{\left(-\frac{1}{3}-1\right)^2 + \left(\frac{7}{3}-1\right)^2} = \frac{2\sqrt{29}}{3}$	Method to find distance between (1, –1) and <b>their</b> centre of the circle	AO1.1a	M1
	$\frac{2\sqrt{29}}{3} > \sqrt{5}$ , so (1, –1) lies outside the circle	Convincing proof with comparison and no errors seen	AO1.1a	A1 <b>[2]</b>
(c)	$\frac{2\sqrt{29}}{3} - \sqrt{5} = \{\text{awrt}\}\ 1.35$	Subtracts <b>their</b> $\sqrt{5}$ from <b>their</b> $\frac{2\sqrt{29}}{3}$ or the other way around	AO1.1a	M1
		Awrt 1.35	AO1.1b	A1 <b>[2]</b>
(d)	$(1)^{2} (7)^{2} 485$	LHS correct	AO1.1b	B1
	$\left(\begin{array}{c}x+\overline{3}\\\end{array}\right)+\left(\begin{array}{c}y-\overline{3}\\\end{array}\right)=\overline{36}$	RHS correct	AO1.1b	B1
				[2]

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(e)	$\sqrt{\frac{485}{36}} - \sqrt{5} > 0$ , so $C_2$ is not completely contained within $C_1$	Correct answer with some justification that the radius of $C_2$ is greater than $C_1$	AO2.1	B1 [ <b>1</b> ]
				11

Question	Scheme	AO	Marks
7			
(a)	$\left(2 - \frac{1}{\sqrt{x}}\right)^8 = 2^8 + \binom{8}{1} (2)^7 \left(-\frac{1}{\sqrt{x}}\right)^1 + \binom{8}{2} (2)^6 \left(-\frac{1}{\sqrt{x}}\right)^2 + \\ + \binom{8}{3} (2)^5 \left(-\frac{1}{\sqrt{x}}\right)^3 + \dots$ See notes for mark breakdown	AO1.1b AO1.1a AO1.1b AO1.1b	B1 M1 A1 A1
	$\left(2 - \frac{1}{\sqrt{x}}\right)^8 = 256 - \frac{1024}{\sqrt{x}} + \frac{1792}{x} - \frac{1792}{\sqrt{x^3}} + \dots$ Correct binomial expansion oe (accept $\frac{1}{\sqrt{x}} = \frac{1}{x^{\frac{1}{2}}} = x^{-\frac{1}{2}}$ etc.)	AO1.1b	A1 oe <b>[5]</b>
(b/i)	$(1+x)^{r} = 1^{r}x^{0} + \binom{r}{1}x^{1} + \binom{r}{2}x^{2} + \dots + 1^{0}x^{r}$ $= 1 + rx + \binom{r}{2}x^{2} + \dots + x^{r}$ Uses the binomial expansion. Need to see 1 and rx appearing clearly. Some candidates may also use $(1+x)^{r} = 1 + rx + \frac{r(r-1)}{2!}x^{2} + \dots$	AO2.1	M1
	$\binom{r}{2}x^2 + \dots + x^r \ge 0$ , since $x > 0$ , so $(1+x)^r \ge 1 + rx$ Convincing proof with an explanation. Accept >.	AO2.4	A1 [2]
(b/ii)	LHS = $(1+0)^r = 1^r = 1$ Correct verification	AO2.1	B1
	RHS = $1+r(0)=1$ LHS = RHS, so true for $x=0$		[1]

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(b/iii)	e.g. let $x = -3$ , then if $r = 5$ , we have LHS = $(1-3)^5 = -32$ RHS = $1+5(-3) = -14$	Attempts to use a suitable counter- example: picks a value of $x < -1$ , substitutes it into the LHS and RHS with a fixed <i>r</i> and attempts to LHS < RHS	AO2.1	M1		
	LHS < RHS, therefore it is not true for $x < -1$ .	Convincing proof with conclusion	AO2.1	A1 <b>[2]</b>		
				10		
	Questic	on 7 Notes				
<b>(a)</b> B1 – sig	nt of 2 <sup>8</sup> as the constant term oe					
1 <sup>st</sup> M1 – terr	m of the form $\binom{8}{r} (2)^{8-r} \left(-\frac{1}{\sqrt{x}}\right)^r$ or equivalent for any $r, r \neq 0$	,8 (in particular, accept $8-r$ and $r$ switch	ed).			
1 <sup>st</sup> A1 – at le	east <b>any</b> two terms of the expansion correct, unsimplified or be	etter				
2 <sup>nd</sup> A1 – the	four terms required terms given, unsimplified or better. Ignore	extra terms				
3 <sup>rd</sup> A1 – cor	rect expansion, with each term simplified. Accept equivalent sin	mplified forms. Ignore extra terms				
SC: first 4 te B1M1A1A0	erms in ascending powers of <i>x</i> (or any other 4 terms given inste A0.	ead of the first 4 descending in <i>x</i> ) can score	e at most			
<b>(b/i)</b> M1 – u without a fin	(b/i) M1 – uses the binomial expansion with the terms 1 and <i>rx</i> clearly appearing. Needs to show one extra term <b>and</b> the final term. '+' without a final term is not sufficient as this can suggest the series is infinite.					
A1 – justifie	A1 – justifies the inequality by stating that the other terms are positive.					
Note: Accep	Note: Accept > instead of $\geq$ .					
<b>(b/iii)</b> M1 – not satisfy tl arbitrary.	(b/iii) M1 – a suitable counter-example: for this mark, candidates need to pick a value of $x < -1$ and attempt to show that this value does not satisfy the inequality for any <b>integer</b> $r$ (i.e. substituting into both sides of the inequality). NOTE: $r$ does not have to be non-negative or arbitrary.					

A1 – complete and convincing proof with a conclusion.

Question	Scheme	AO	Marks
8			
(a)	$2x - 4y = 10 \Rightarrow y =$ Attempts to make y the subject	AO1.1a	M1
	$y = \frac{1}{2}x - \frac{5}{2}$ , so $m_{l_2} = \frac{1}{2}$		
	$\Rightarrow m_{l_1} = -2$ Correct gradient of $l_1$	AO1.1b	A1 <b>[2]</b>
	Credit in (c) can be given for work in (b), but credit in (b) cannot be given for work in (c)		
(b)	$l_1: y = -2x + c$ , so $A\left(\frac{c}{2}, 0\right)$ , $B(0, c)$ Attempts to find expressions for the points A and B	AO3.1a	M1
	$\frac{1}{2}\left(\frac{c}{2}\right)(c) = 4 \Rightarrow c^2 = 16$ Attempts to use area of right-triangle formula with their A and B co/ords	AO2.2	M1
	Correct expression: $c^2 = 16$	AO1.1b	A1
	$\Rightarrow c = -4  \{c \neq 4\}$		
	A(-2,0), B(0,-4) Correct coordinates of A and B	AO2.2	A1 <b>[4]</b>

(c)	$y = -2x - 4 \Longrightarrow 2x + y + 4 = 0 \{k = 4\}$	Substitutes their y coordinate of B as 'c' in the equation of $l_1$	AO1.1a	M1
		Correct equation of $l_1$ in required form or value of <i>k</i> stated. Value of <i>k</i> stated alone is <b>2/2</b>	AO1.1b	A1 <b>[2]</b>
(d)	$D\left(0,-\frac{5}{2}\right)$	Correct coordinates of D	AO3.1a	B1
	e.g. $-2x - 4 = \frac{1}{2}x - \frac{5}{2} \Longrightarrow x =$	Attempts to find the coordinates of <i>C</i> by solving <b>their</b> equation for $l_1$ and the equation of $l_2$ simultaneously. Can be implied by correct coordinates	AO3.1a	M1
	$C\left(-\frac{3}{5},-\frac{14}{5}\right)$	Correct coordinates of C	AO1.1b	A1
	Area of <i>OACD</i> = area of <i>OAB</i> – area of <i>BCD</i> Area of <i>BCD</i> = $\frac{1}{2} \left( \frac{3}{5} \right) \left( 4 - \frac{5}{2} \right) = \frac{9}{20}$	Area of <i>BCD</i> with subtraction seen (using their <i>C</i> and <i>D</i> )	AO3.1a	dM1
	$\Rightarrow$ area of OACD = $4 - \frac{9}{20} = \frac{71}{20}$	Correct area	AO2.1	A1 <b>[5]</b>
				13

	Question 8 Notes		
(d) 2 <sup>nd</sup> M1 – there are likely to be many ways to find the area of the quadrilateral. For this mark, candidates need to calculate the relevant, unknown areas involved using their C and/or D, and then show use of subtraction/addition.			
Alternative both the are	for (d): 2 <sup>nd</sup> M1 – can split the quadrilateral OACD into a right-triangle and a trapezium. M mark is for attempting to calculate a of the trapezium and triangle (ft their C and/or D) and adding these together.		